

# Qualitative Comparative Analysis

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97th Annual Meeting of the  
Southwestern Social Science Association  
Austin, Texas  
April 14, 2017

# Overview

- Review of QCA publications and software
- QCA as an investigation of invariance
- Three analytic components of QCA
  - Data set calibration
  - Necessity analysis
    - Consistency and coverage measures for necessity
    - Testing for necessary conditions
  - Sufficiency analysis
    - Consistency and coverage measures for sufficiency
    - Constructing and reducing truth tables
- Interrogating the solutions

# Primary Readings on QCA

- Ragin (2008) *Redesigning Social Inquiry*
- Ragin (1987) *The Comparative Method*
- Ragin and Rubinson (2009) “The Distinctiveness of Comparative Research”
- Ragin and Rubinson (2011) “Comparative Methods”

## Secondary Sources

- COMPASSS web site (<http://www.compassss.org>)
- Goertz and Mahoney (2012) *A Tale of Two Cultures*
- Ragin and Fiss (2016) *Intersectional Inequality*
- Goertz (2006) *Social Science Concepts*
- Ragin (2000) *Fuzzy-Set Social Science*
- Schneider and Wagemann (2012) *Set-Theoretic Methods for the Social Sciences*
- Rihoux and Ragin (2009) *Configurational Comparative Methods*

# Major Software Packages

(complete list at <http://ww.compass.org>)

QCA

(Drass and Ragin 1992)

TOSMANA  
(Cronqvist 2016)

fs/QCA

(Ragin, Drass, and Davey 2016)

QCA3 (R)  
(Huang 2016)

QCA (R)  
(Dusa 2017)

QCApro (R)  
(Thiem 2016)

fuzzy (Stata)  
(Longest and Vaisey 2008)

Kirq & acq

(Rubinson and Reichert 2014)

# Varieties of QCA: csQCA, fsQCA, and mvQCA

- *The Comparative Method* (1987) describes “crisp-set QCA”
- *Fuzzy-Set Social Science* (2000) describes “fuzzy-set analysis”
- *Redesigning Social Inquiry* (2008) unifies “crisp-set QCA” and “fuzzy-set QCA”
  - csQCA is a special form of fsQCA
  - *fs/QCA*, *acq/Kirq*, and R packages are all based on the RSI algorithms
- What about multi-valued QCA?

# What is QCA?

- QCA is a formalization of the comparative method, using Boolean algebra

## What is the comparative method?

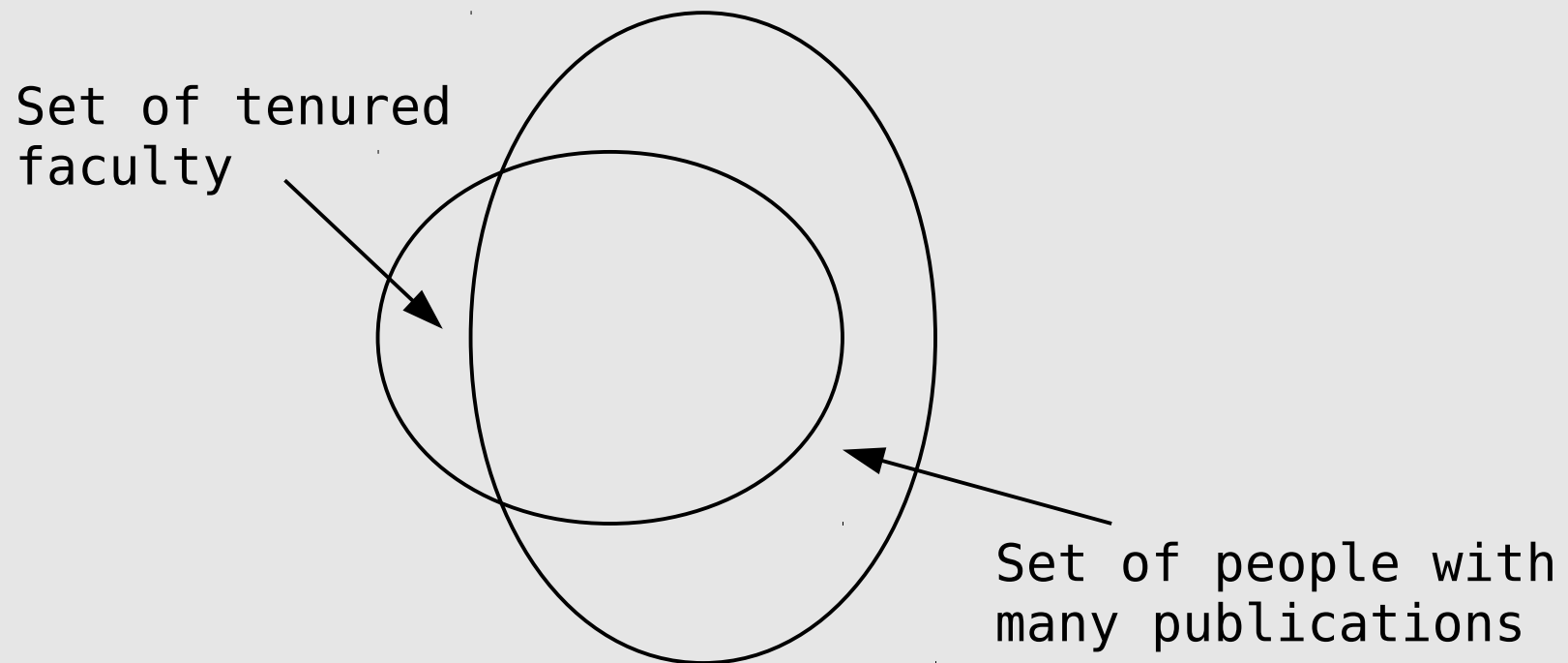
- Many names: comparative research, comparative analysis, small-N comparison, small-N analysis, case studies, cross-case studies
- Is a technique for identifying and analyzing invariant (consistent) relationships.
- Characterized by the search for necessary and sufficient conditions.
- Is comparative research necessarily small-N?
- Is comparative research necessarily case-oriented?

# Invariant Relationships

- Definition: Certain aspects of cases tend to co-occur.
  - Tenured faculty tend to have many publications
  - Religious fundamentalists tend to be politically conservative
  - “business leaders and owners of capital ... are overwhelmingly Protestant” (Weber 1958:35)
  - “No bourgeois, no democracy.” (Moore 1966:418)

# Invariant Relationships

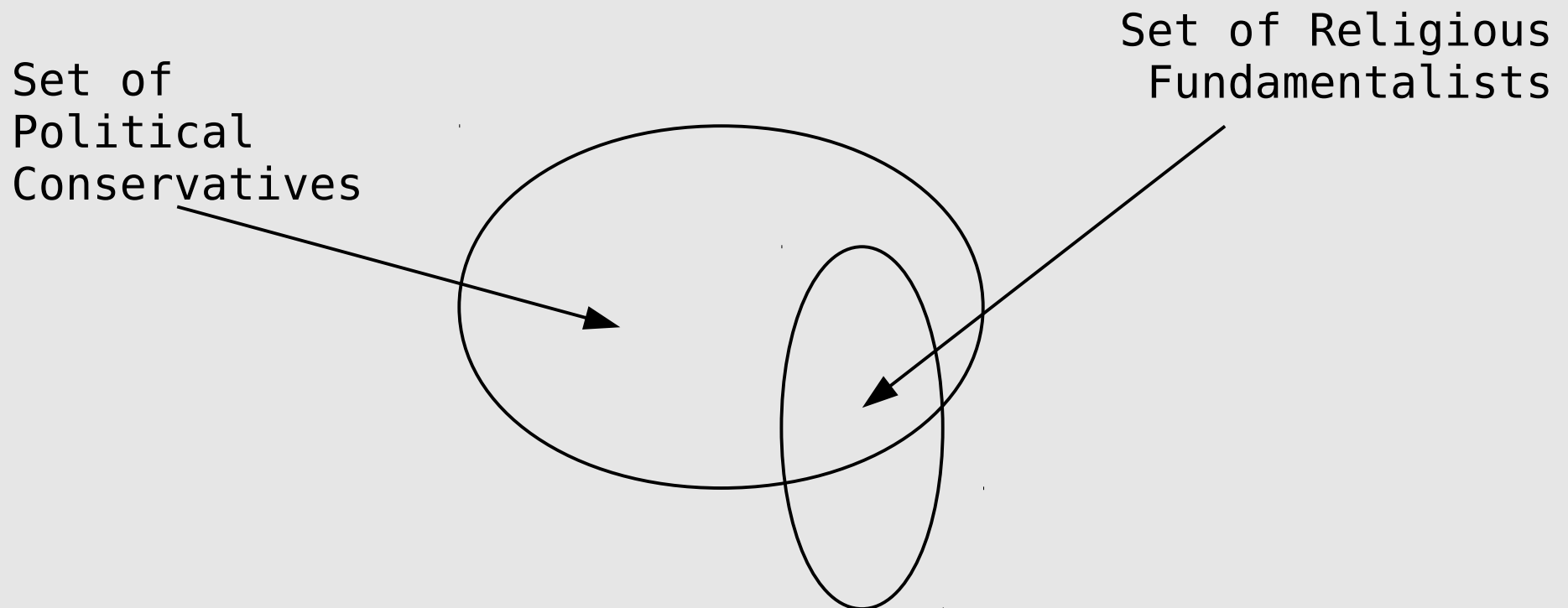
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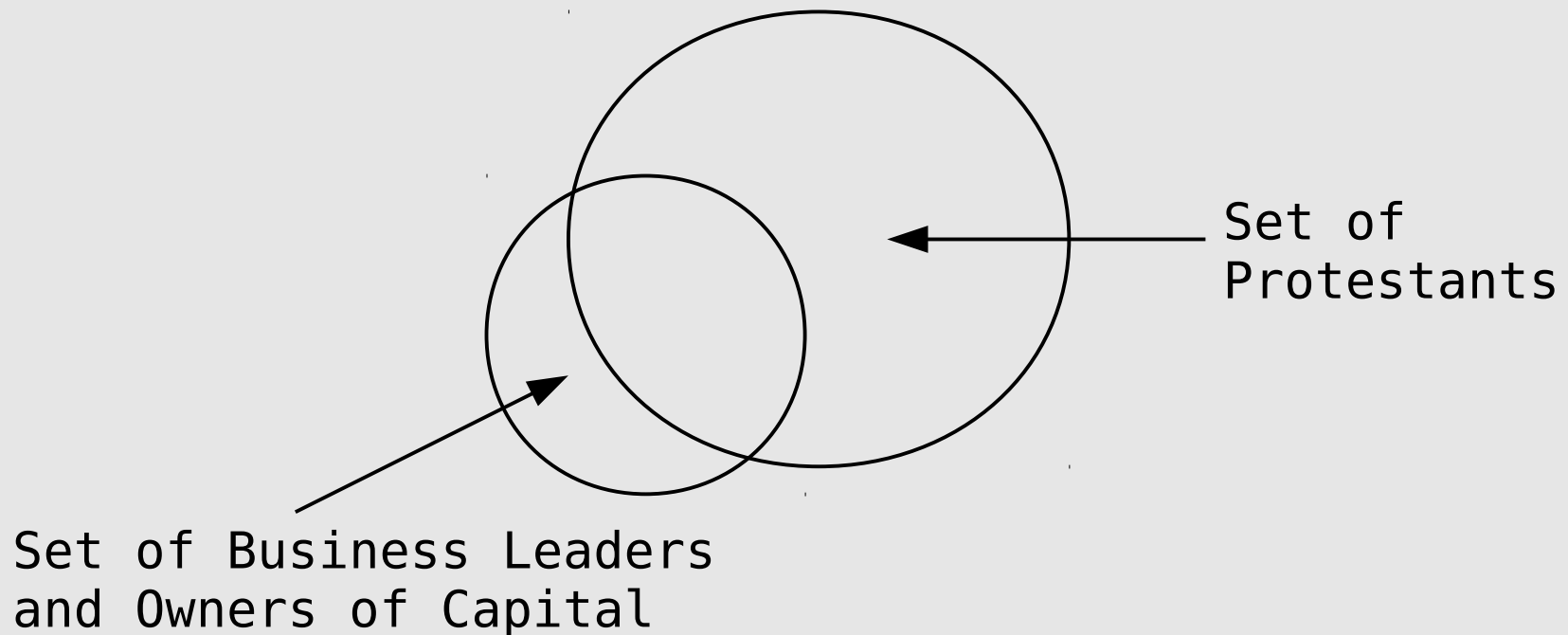
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# Invariant Relationships

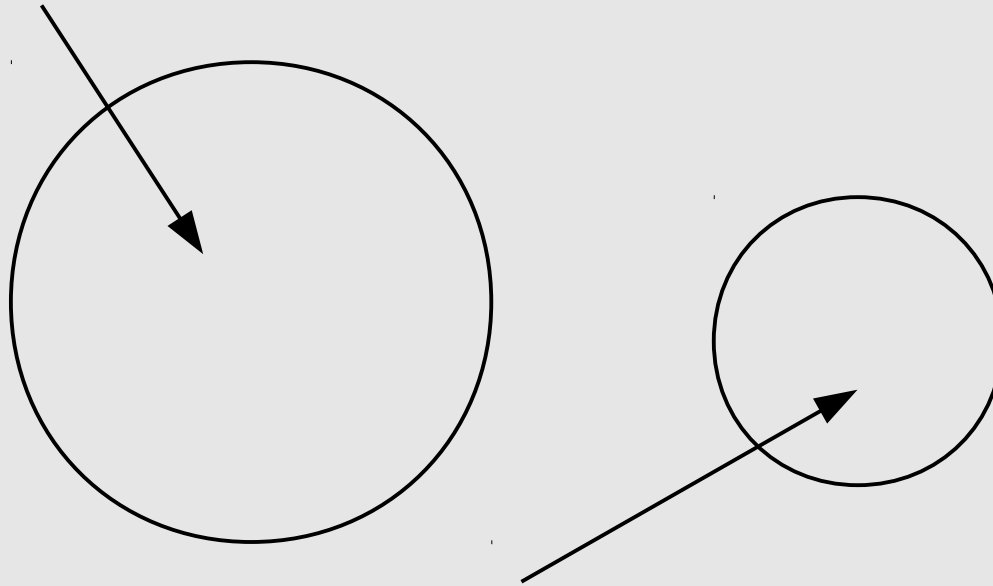
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# Invariant Relationships

- Definition: Certain aspects of cases tend to co-occur.
  - “No bourgeois, no democracy.” (Moore 1966:418)

Set of Countries **without** a Strong Bourgeois Impulse

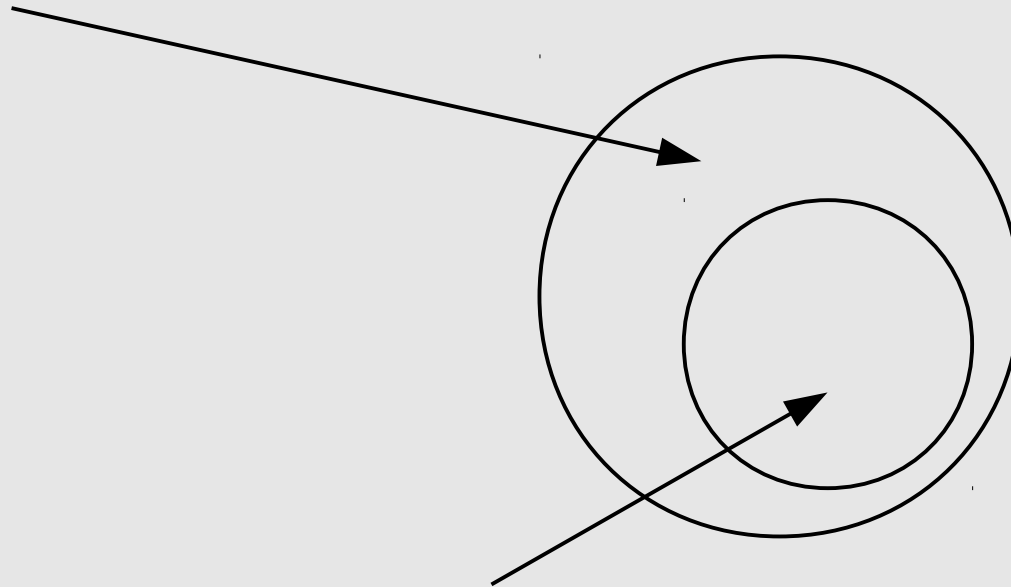


Set of Countries that Experienced a Bourgeois Revolution

# Invariant Relationships

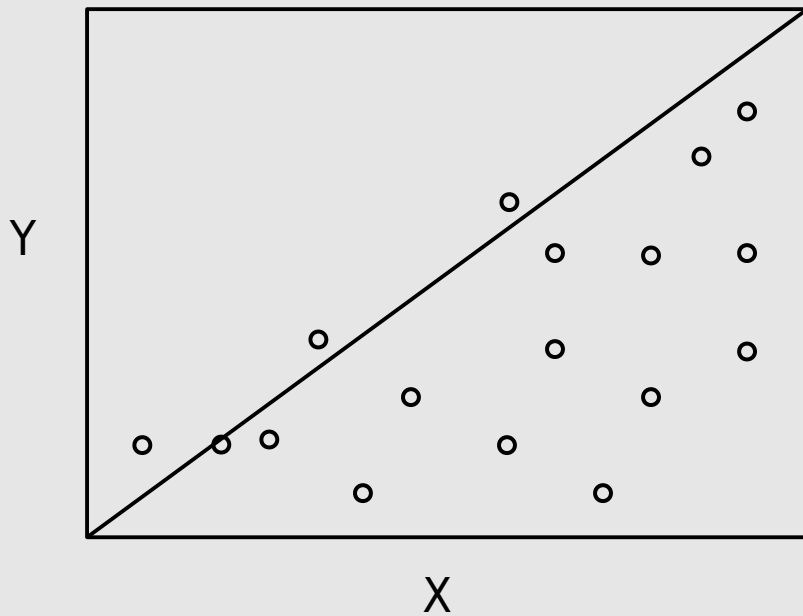
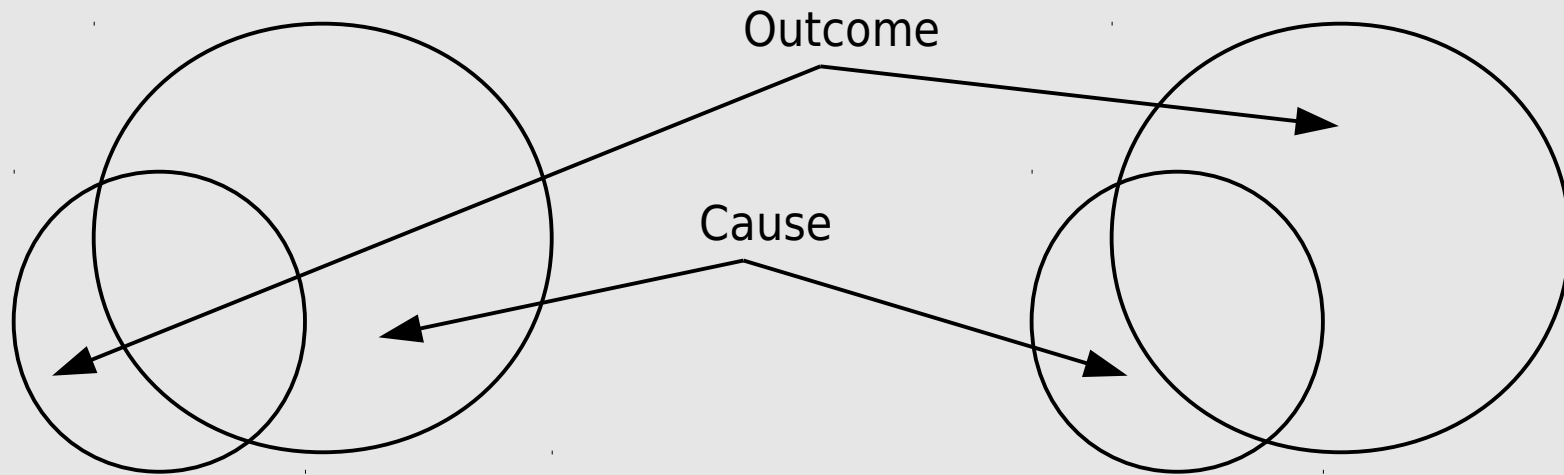
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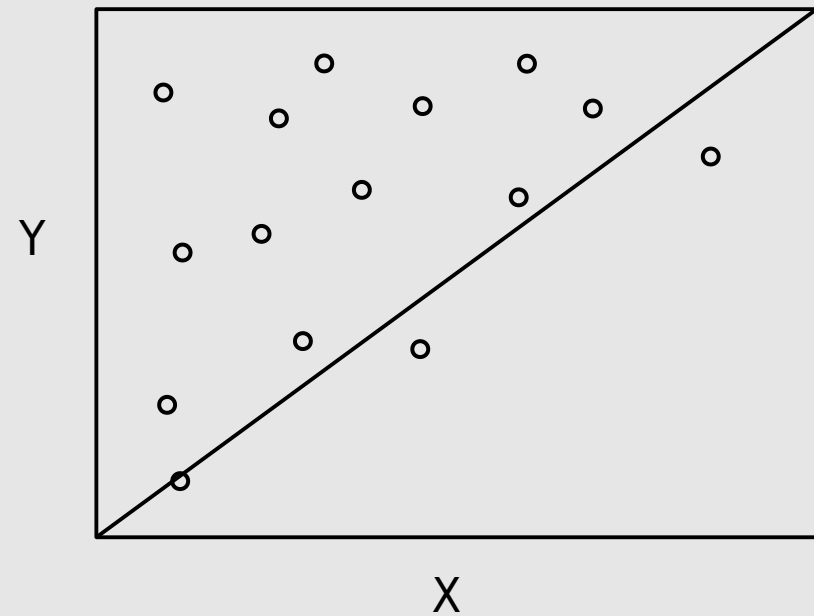


Set of Countries that Experienced a Bourgeois Revolution

# Invariant Relationships



Subset relationship consistent with *necessity* ( $X \geq Y$ )



Subset relationship consistent with *sufficiency* ( $Y \geq X$ )

# Invariant Relationships

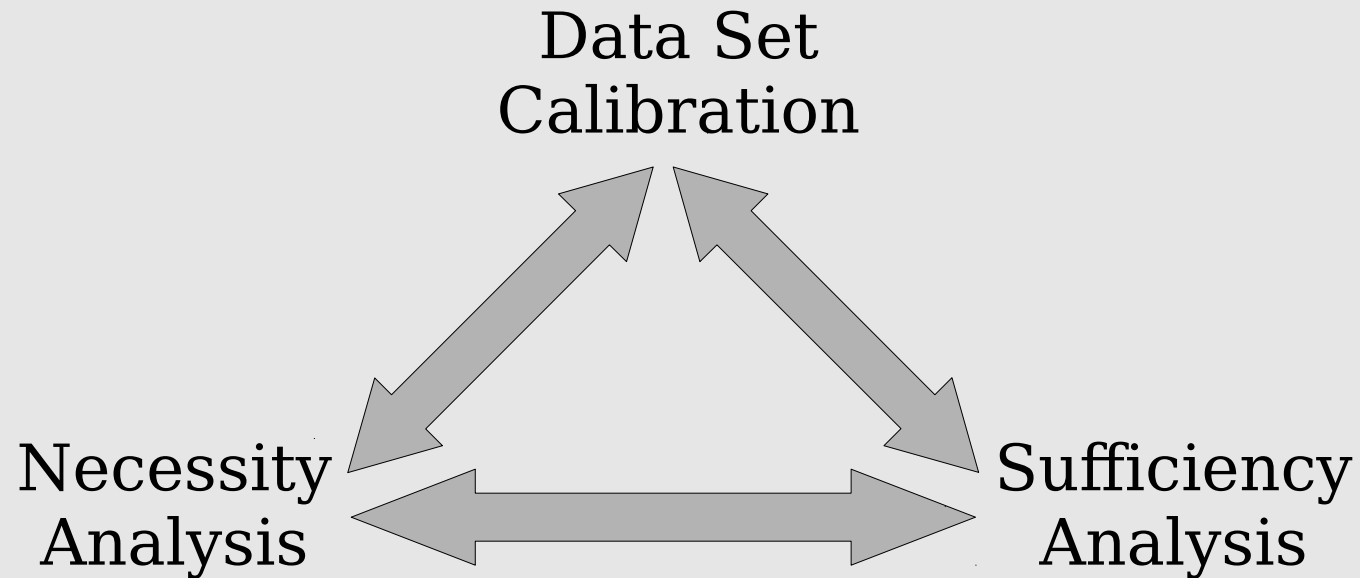
- Definition: Certain aspects of cases tend to co-occur.
  - Does not imply determinism (or stochasticism)
  - Is not vulnerable to a single disconfirming case
  - Is fundamentally set-theoretic
  - Parallels how we typically formulate social theory:
    - The modern world system is a capitalist world-economy characterized by a core/periphery division of labor that prioritizes the endless accumulation of capital.
    - During unsettled periods, people actively use culture to learn new ways of being.



# Software Demonstration

## Example: Brown and Boswell (1995)

# Three Analytic Components of QCA





# Boolean Algebra

- UPPERCASE for the presence of a condition
- lowercase for the absence of a condition
- Negation
$$\sim A = 1 - A$$
$$a = 1 - A$$
- Logical and (Boolean multiplication)
$$A \cdot b = Ab = \min(A, b)$$
- Logical or (Boolean addition)
$$A + b = \max(A, b)$$

# Calibrating Data Sets

# Data Set Calibration

- The process of constructing fuzzy-sets
- May be crisp or fuzzy
- Is about defining set memberships
  - degree of membership in the set of rich people (vs annual income)
  - degree of membership in the set of developed countries (vs GDP/capita)
- Importance of negation and asymmetry
  - degree of membership in the set of *not* rich people
  - degree of membership in the set of *not* developed countries

# Data Set Calibration

- Instrument calibration is routine in the natural sciences; largely absent in the social sciences.
- Conventional statistics emphasize relative effects: Paul is poorer than Peter; the United States' infant mortality rate is greater than that of Japan.
- Calibration allows us to state that an individual is poor or that a country's infant mortality rate is high.
- Calibration requires application of theoretical and substantive knowledge: What does it mean to classify a country as partially versus fully democratic?

# Calibrating Fuzzy Sets

Crisp set	Three-value fuzzy set	Four-value fuzzy set	Six-value fuzzy set	Continuous fuzzy set
1 = fully in	1 = fully in	1 = fully in	1 = fully in	1 = fully in
	0.67 = more in than out	0.67 = more in than out	0.8 = mostly but not fully in	Degree of membership is more "in" than "out"
			0.6 = more or less in	$0.5 < X < 1$
----- 0.5 = Crossover Point -----				
			0.4 = more or less out	Degree of membership is more "out" than "in"
		0.33 = more out than in	0.2 = mostly but not fully out	$0.0 < X < 0.5$
0 = fully out	0 = fully out	0 = fully out	0 = fully out	0 = fully out

# Analyzing Necessary Conditions

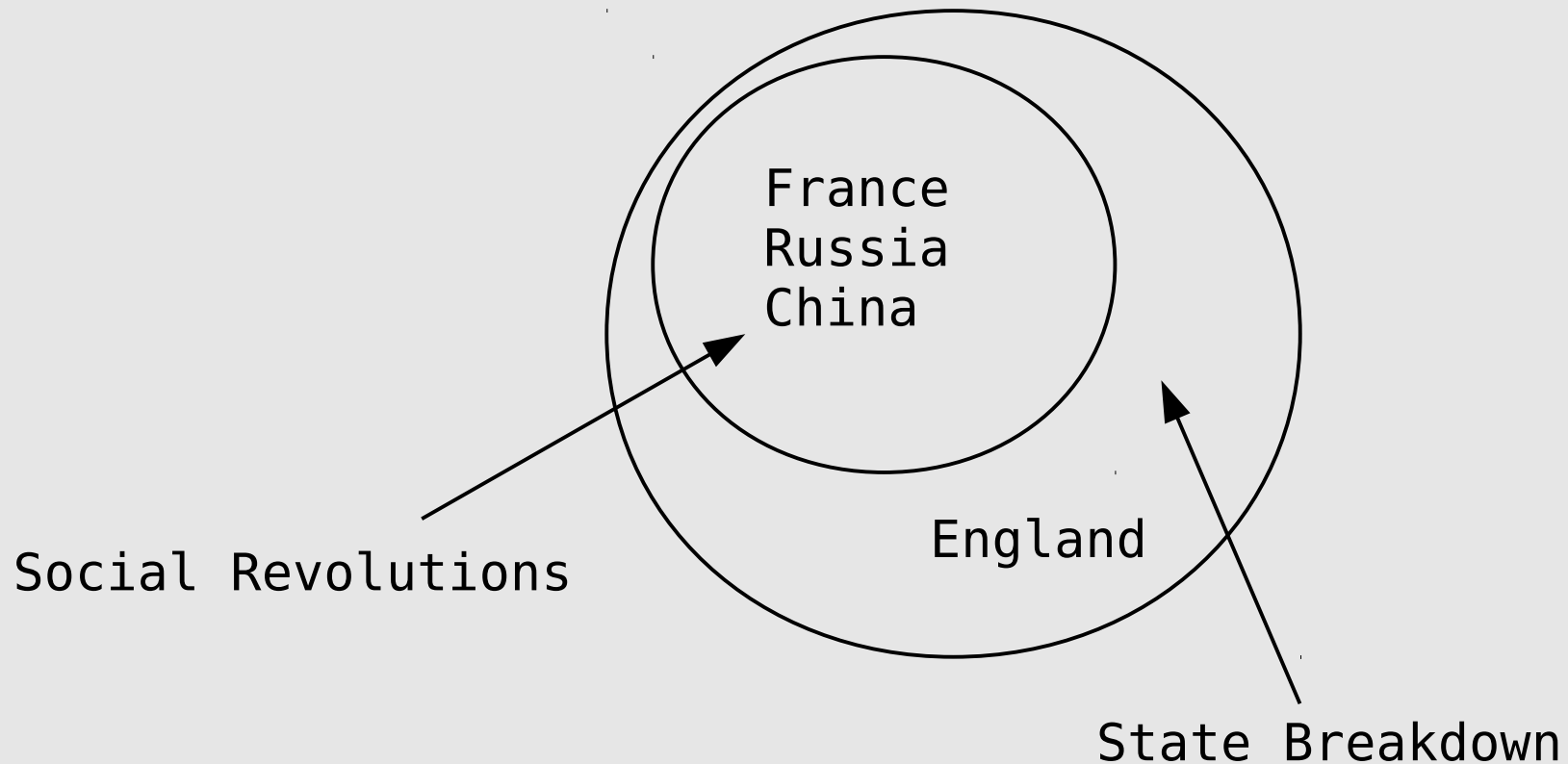
# Necessity Analysis

- Underdeveloped in the literature; QCA development has focused on sufficiency analysis
- Kirq and acq have sophisticated necessity testing

# Necessary Conditions

Causal condition must (almost always) be present for outcome to occur.

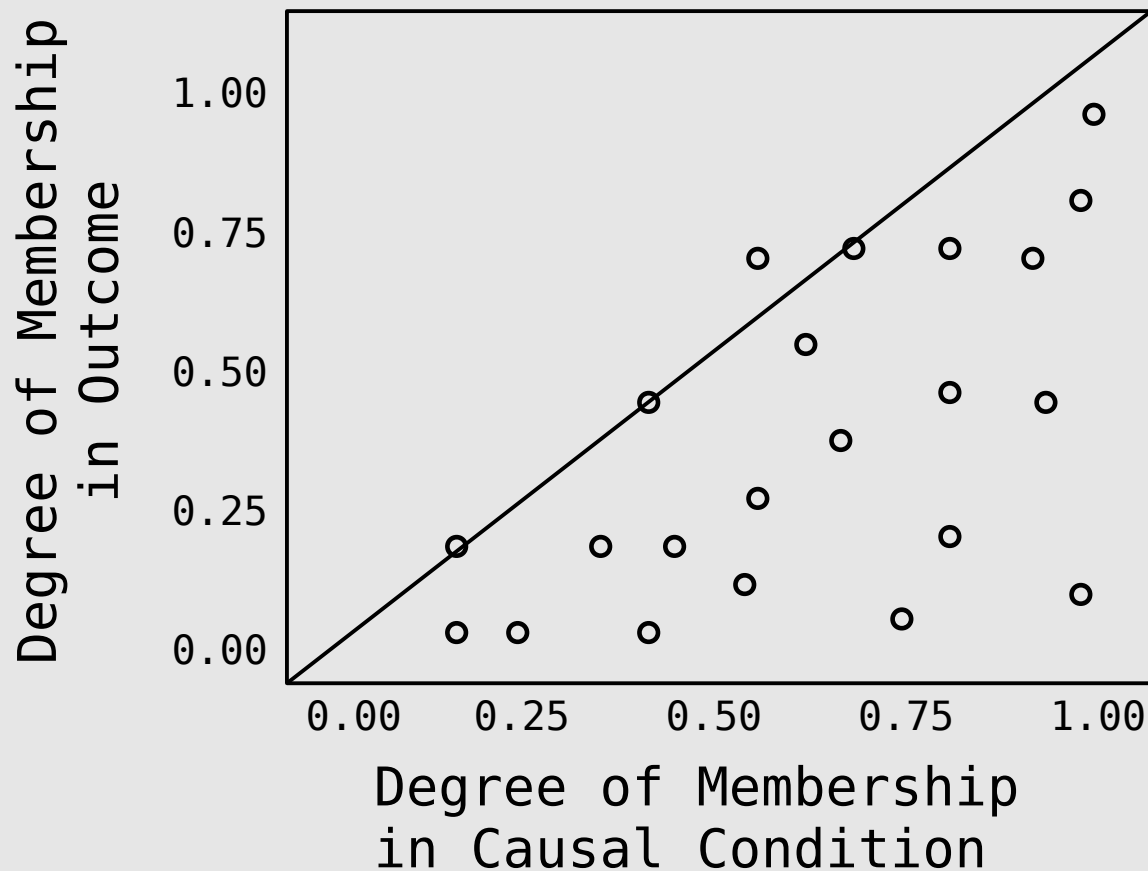
Outcome is a subset of Cause





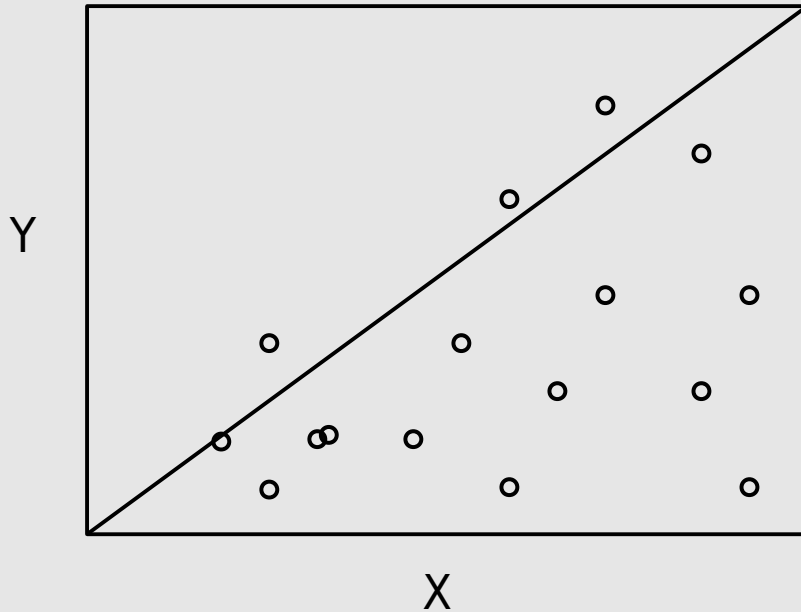
# Fuzzy Subset Relationship Consistent with Necessity

Outcome is a subset of Cause ( $X \geq Y$ )

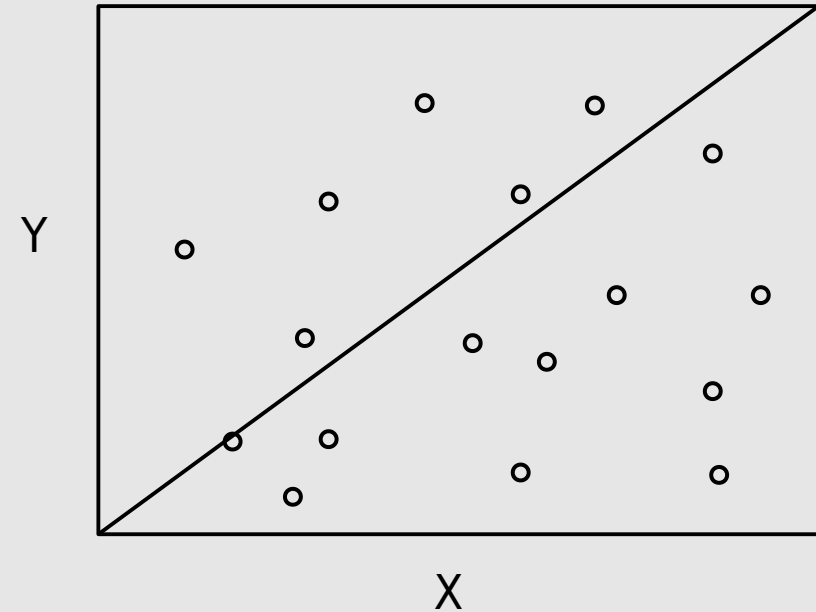


# Assessing Necessary Conditions

- *Consistency* measures degree to which subset relationship is “consistent” with necessity



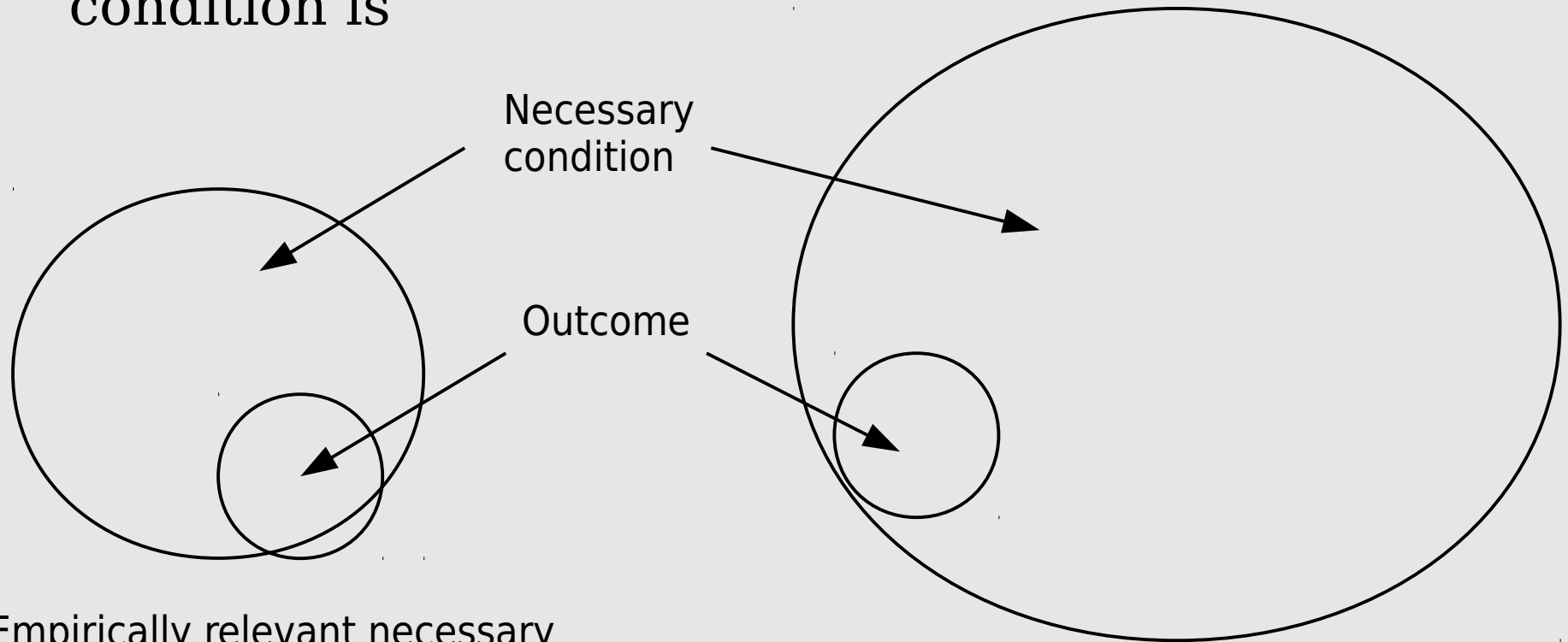
Subset relationship consistent with necessity



Subset relationship with substantial inconsistency

# Assessing Necessary Conditions

- *Coverage* measures how “relevant” a necessary condition is

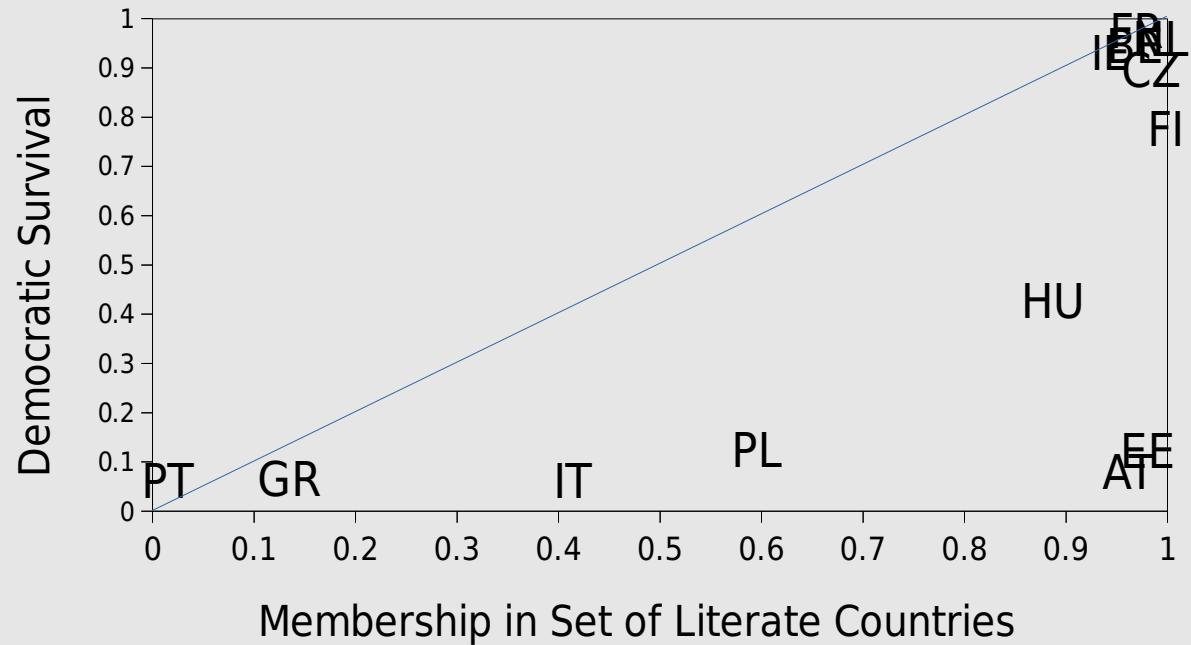


Empirically relevant necessary condition (high consistency)

Empirically irrelevant necessary condition (perfect consistency)

# Testing for Necessary Conditions

Obs	Dev	Urb	Lit	Sur
AT	.81	.12	.99	.05
BE	.99	.89	.98	.95
CZ	.58	.98	.98	.89
EE	.16	.07	.98	.12
FI	.58	.03	.99	.77
FR	.98	.03	.99	.95
DE	.89	.79	.99	.05
GR	.04	.09	.13	.06
HU	.07	.16	.88	.42
IE	.72	.05	.98	.92
IT	.34	.10	.41	.05
NL	.98	1.00	.99	.95
PL	.02	.17	.59	.12
PT	.01	.02	.01	.05



Term	Consis	Cov
LIT	0.99	0.58
Solution	0.99	0.58

# Testing for Necessary Conditions

- Assess consistency before coverage
- Join terms with logical or (e.g.,  $A+B+C$ )
- Many solutions are possible
- Use of theory is crucial

# Analyzing Sufficient Conditions

# Sufficiency Analysis

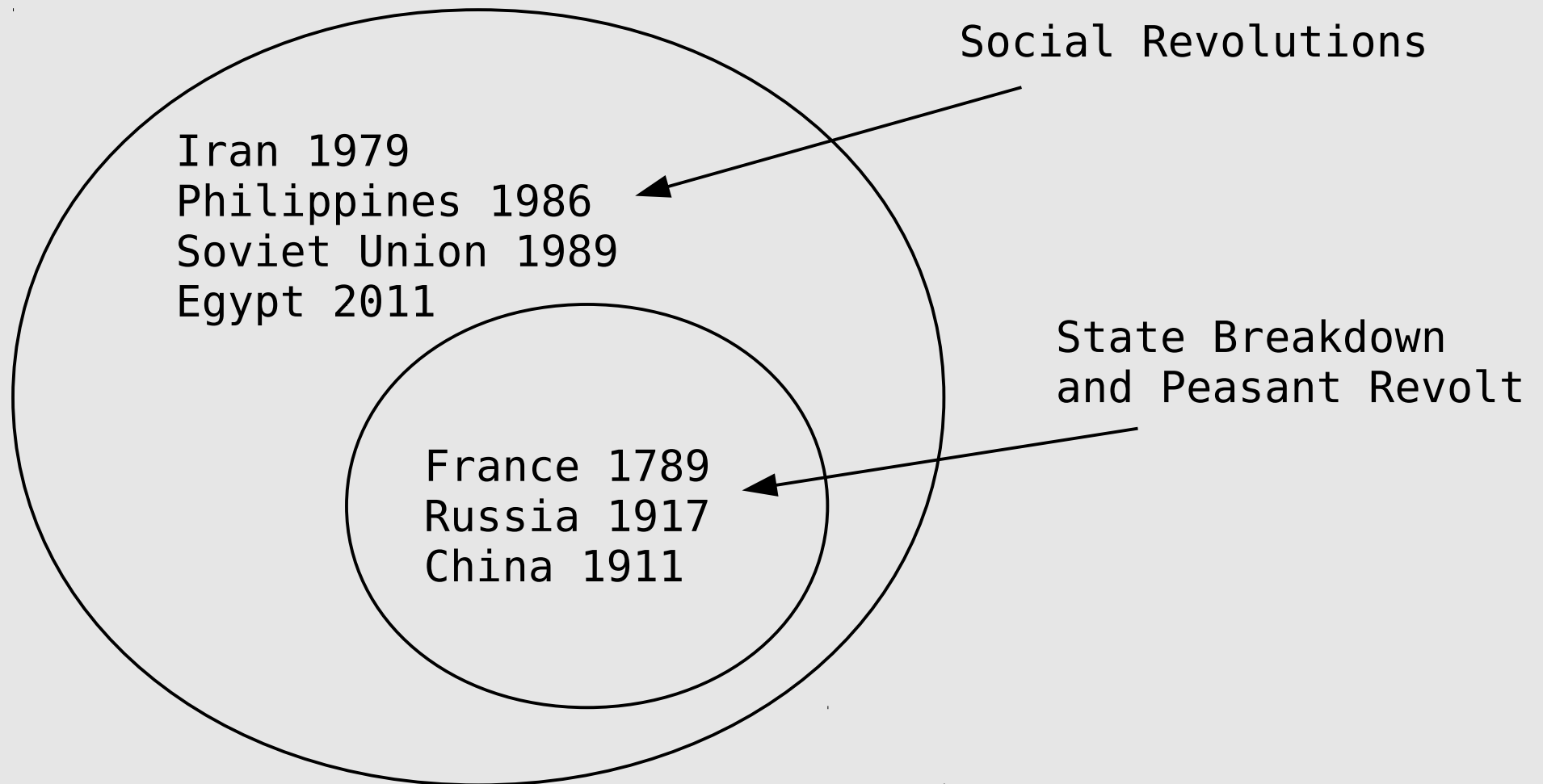
- More mature than necessity analysis; QCA development—and applications—have focused on sufficiency analysis
- Emphasis on causal complexity (a.k.a., multiple conjunctural causation, “recipes,” equifinality, or INUS conditions)

Feature	fs/QCA	Kirq & acq
Based on RSI Algorithms	✓	✓
Complex Solutions	✓	✓
Intermediate Solutions	✓	
Parsimonious Solutions	✓	✓
Impossible Conditions		✓
Contradictions		✓

# Sufficient Conditions

Outcome (almost) always occurs when causal condition is present.

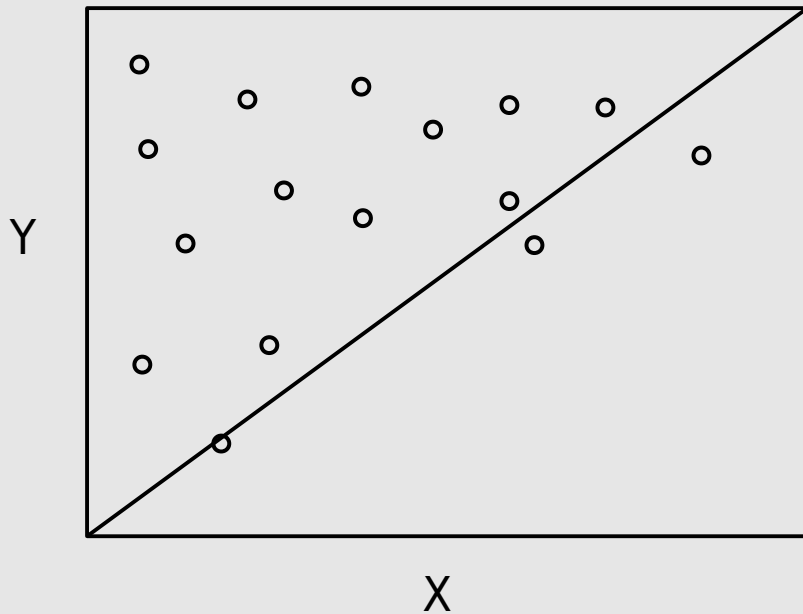
Cause is a subset of Outcome



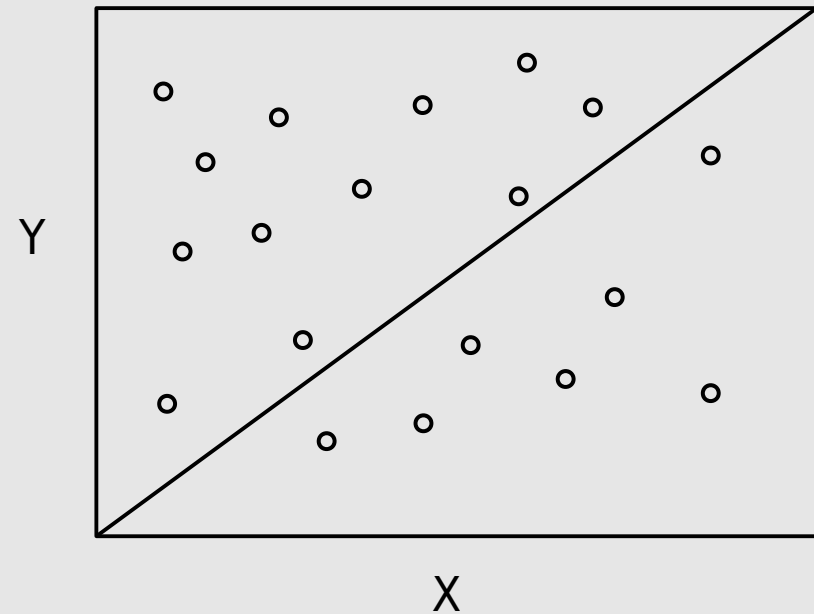


# Assessing Sufficient Conditions

- *Consistency* measures degree to which subset relationship is “consistent” with sufficiency



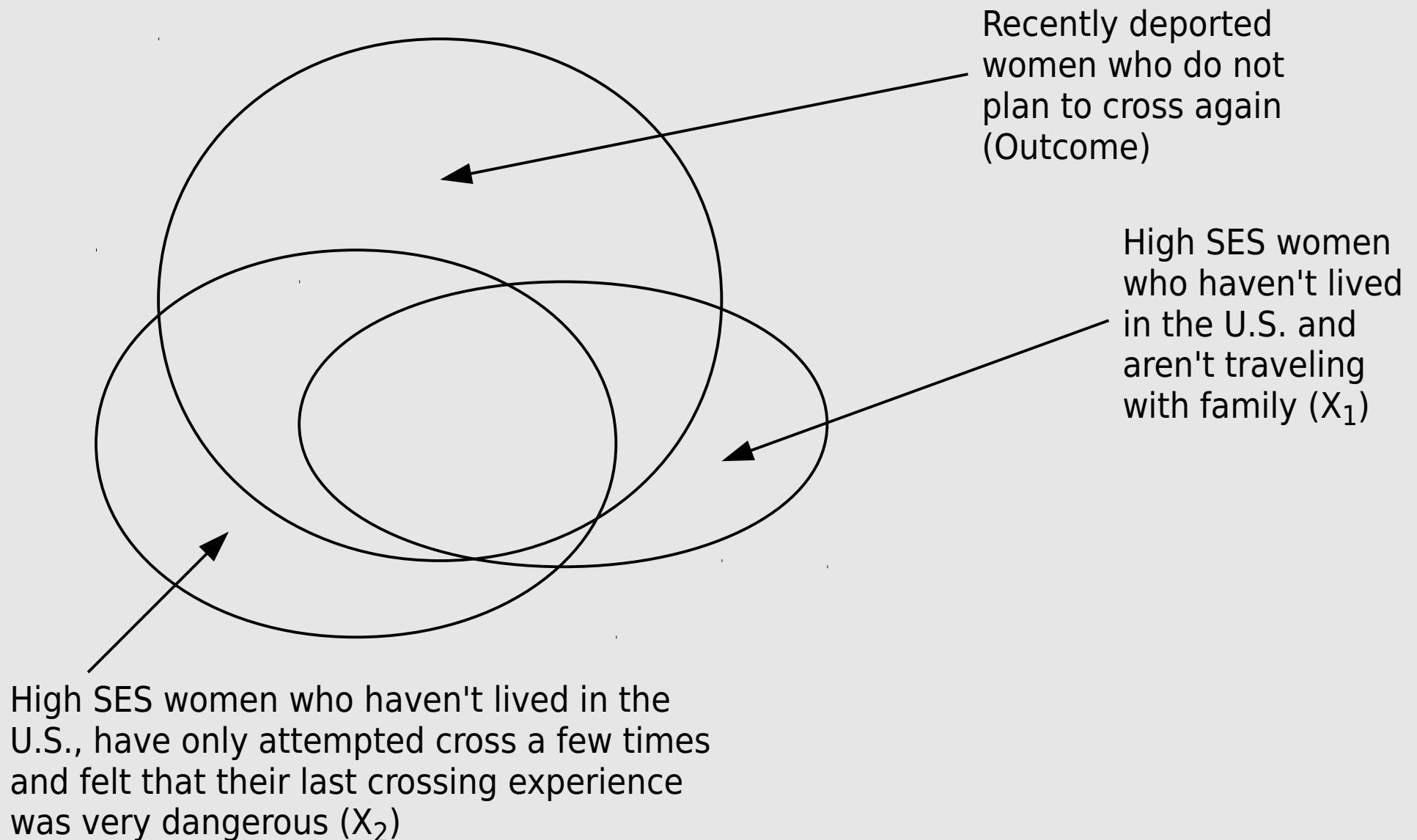
Subset relationship consistent with sufficiency



Subset relationship with substantial inconsistency

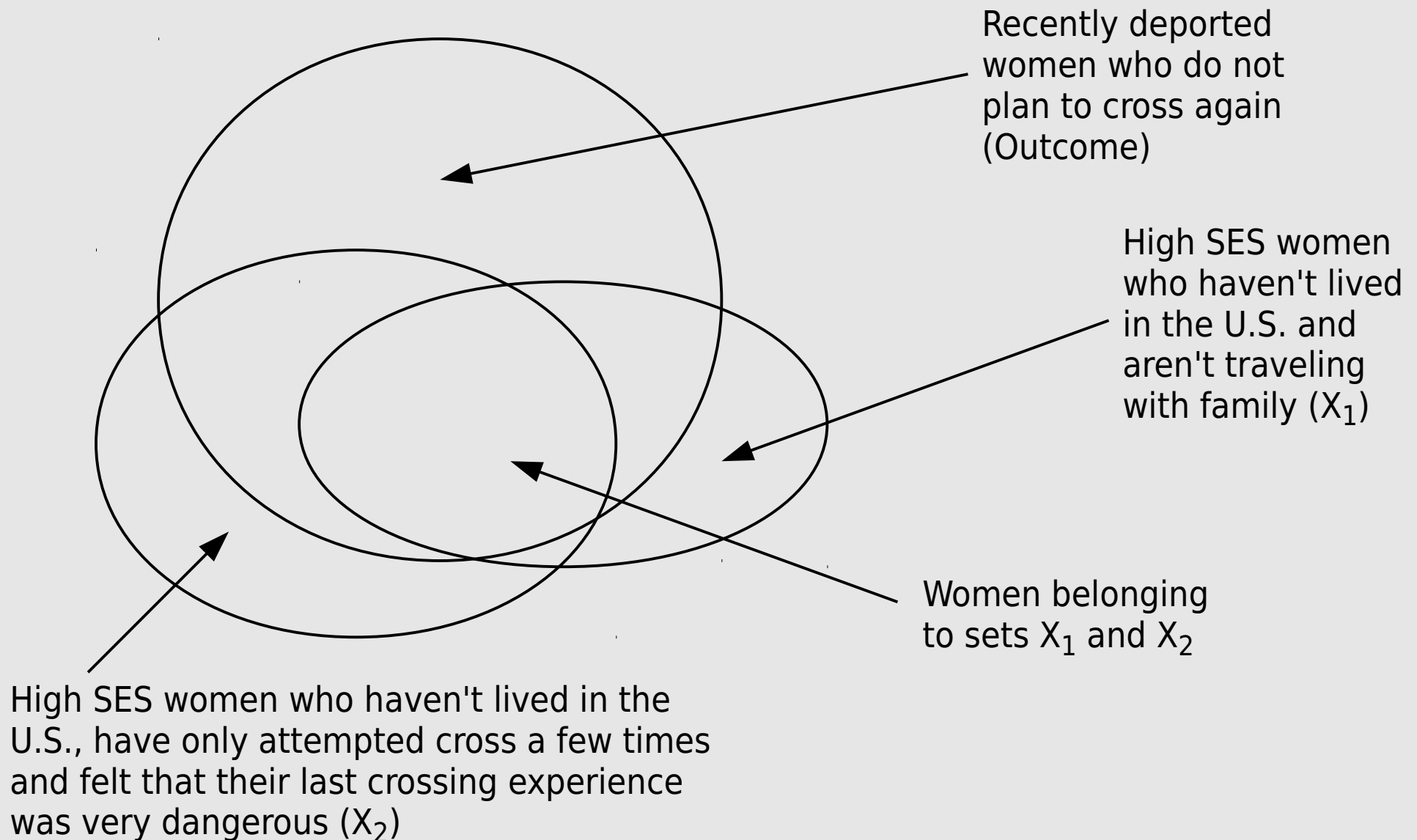
# Assessing Sufficient Conditions

- *Coverage* measures the relative “importance” of each solution



# Assessing Sufficient Conditions

- *Coverage* measures the relative “importance” of each solution



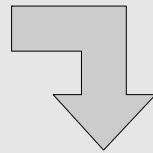
# Testing for Sufficient Conditions

Term	Consis	Raw Cov	Uniq Cov
HISES*liveus*travfam +	0.90	0.32	0.13
HISES*liveus*numcross*DANGER	0.82	0.48	0.26
Solution	0.86	0.58	

# Truth Table Construction

Truth table algorithm sorts observations into types

Obs	Dev	Urb	Lit	Brk
AT	.81	.12	.99	.95
BE	.99	.89	.98	.05
CZ	.58	.98	.98	.11
EE	.16	.07	.98	.88
FI	.58	.03	.99	.23
FR	.98	.03	.99	.05
DE	.89	.79	.99	.95
GR	.04	.09	.13	.94
HU	.07	.16	.88	.58
IE	.72	.05	.98	.08
IT	.34	.10	.41	.95
NL	.98	1.00	.99	.05
PL	.02	.17	.59	.88
PT	.01	.02	.01	.95



	Dev	Urb	Lit	Consis	Y	Consis	Obs	Inconsis	Obs
1	T	T	T	0.41	F	DE			BE, CZ, NL
2	T	T	F	—	—				
3	T	F	T	0.51	F	AT			FI, FR, IE
4	T	F	F	—	—				
5	F	T	T	—	—				
6	F	T	F	—	—				
7	F	F	T	0.83	T	EE, PL			HU
8	F	F	F	0.99	T	GR, IT, PT			

# Reading Truth Tables

Truth table assesses consistency between types and outcome

Democracy usually did not break down in countries that were (a) developed, urbanized, and literate (row 1) or (b) developed, not urbanized, and literate (row 3).

Democracy usually did break down in countries that were (c) not developed, not urbanized, and literate (row 7) or (d) not developed, not urbanized, and not literate (row 8)

	Dev	Urb	Lit	Consis	Y	Consis	Obs	Inconsis	Obs
1	T	T	T	0.41	F	DE		BE, CZ, NL	
2	T	T	F	—	—				
3	T	F	T	0.51	F	AT		FI, FR, IE	
4	T	F	F	—	—				
5	F	T	T	—	—				
6	F	T	F	—	—				
7	F	F	T	0.83	T	EE, PL		HU	
8	F	F	F	0.99	T	GR, IT, PT			

# Reading Truth Tables

Remainders are logically possible conditions lacking empirical instances

Remainders

	Dev	Urb	Lit	Consis	Y	Consis	Obs	Inconsis	Obs
1	T	T	T	0.41	F	DE		BE, CZ, NL	
2	T	T	F	—	—				
3	T	F	T	0.51	F	AT		FI, FR, IE	
4	T	F	F	—	—				
5	F	T	T	—	—				
6	F	T	F	—	—				
7	F	F	T	0.83	T	EE, PL		HU	
8	F	F	F	0.99	T	GR, IT, PT			

# Invariance in Truth Tables

	Dev	Urb	Consis	Y	Consis Obs	Inconsis Obs
1	T	T	0.41	F	DE	BE, CZ, NL
2	T	F	0.51	F	AT	FI, FR, IE
3	F	T	—	—		
4	F	F	0.89	T	EE, GR, IT, PL, PT	HU

	Dev	Urb	Lit	Consis	Y	Consis Obs	Inconsis Obs
1	T	T	T	0.41	F	DE	BE, CZ, NL
2	T	T	F	—	—		
3	T	F	T	0.51	F	AT	FI, FR, IE
4	T	F	F	—	—		
5	F	T	T	—	—		
6	F	T	F	—	—		
7	F	F	T	0.83	T	EE, PL	HU
8	F	F	F	0.99	T	GR, IT, PT	



# Reducing Truth Tables to Boolean Equations

To Primitive Expressions:

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb*LIT +	0.83	0.42	0.27	EE, PL, [HU]
dev*urb*lit	0.99	0.40	0.24	GR, IT, PT
Solution	0.88	0.66		

# Reducing Truth Tables to Boolean Equations

To Primitive Expressions:

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb*LIT +	0.83	0.42	0.27	EE, PL, [HU]
dev*urb*lit	0.99	0.40	0.24	GR, IT, PT
Solution	0.88	0.66		

To Prime Implicants:

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb	0.89	0.71	0.71	EE, PL, GR, IT, PT, [HU]
Solution	0.89	0.71		

# Reducing Truth Tables to Boolean Equations

Reduce Prime Implicants (Complex Solution):

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb	0.89	0.71	0.71	EE, PL, GR, IT, PT, [HU]
Solution	0.89	0.71		

# Reducing Truth Tables to Boolean Equations

Reduce Prime Implicants (Complex Solution):

Term	Consis	Raw Cov	Uniq Cov	Observations
dev*urb	0.89	0.71	0.71	EE, PL, GR, IT, PT, [HU]
Solution	0.89	0.71		

Reduce Prime Implicants Using Remainders (Parsimonious Solution):

Term	Consis	Raw Cov	Uniq Cov	Observations
dev	0.82	0.73	0.73	EE, PL, GR, IT, PT, [HU]
Solution	0.82	0.73		

# Constructing Intermediate Solutions (Counterfactual Analysis with QCA)

Complex Solution

Acsir +  
ACSir +  
ASIR

Parsimonious Solution

i +  
SR

Intermediate Solution #1

Ai +  
ACSi +     →     Ai +  
ASR                    ASR

Intermediate Solution #2

Air +  
ASIR

# Factoring Results

Initial Solution:

$$\begin{aligned} & \text{ELECTIONS} * \text{POLICE} + \\ & \text{urban} * \text{POLICE} + \\ & \text{CONFLICT} * \text{ELECTIONS} * \text{URBAN} + \\ & \text{CONFLICT} * \text{elections} * \text{urban} + \\ & \text{conflict} * \text{ELECTIONS} * \text{urban} \end{aligned}$$

Factored Solution:

$$\begin{aligned} & \text{POLICE} (\text{ELECTIONS} + \text{urban}) + \\ & \text{URBAN} (\text{CONFLICT} * \text{ELECTIONS}) + \\ & \text{urban} ((\text{CONFLICT} * \text{elections}) + (\text{conflict} * \text{ELECTIONS})) \end{aligned}$$

# Visualizations

Goals of QCA visualization:

- Present superset/subset relationships
- Preserve case holism and diversity
- Clarify configurations
- Convey range of solution complexity

Examples:

- 2x2 tables (crisp sets) & scatterplots (fuzzy sets)
- Venn/Euler diagrams (area-proportional)
- Fiss configuration charts